displaced by one octahedron diagonal with respect to each other. This linkage is the same as that occurring in one of the Nb<sub>2</sub>O<sub>5</sub> modifications, namely N-Nb<sub>2</sub>O<sub>5</sub> (Andersson, 1967*b*).

In conclusion we note that electron diffraction and crystal structure imaging techniques have been of paramount importance in the deduction of a plausible structure of NaNb<sub>7</sub>O<sub>18</sub>. These results will serve as a good starting point for a more accurate structure determination, should X-ray single-crystal diffraction data become available in the future. We also think that continued studies using HREM of NaNb<sub>7</sub>O<sub>18</sub> or similar compounds will reveal further types of structural defects. Such work is now under way.

We wish to express our thanks to Professor Lars Kihlborg for his continuous interest in this work



Fig. 6. HREM image of a thin crystal flake illustrating a second type of defect observed in NaNb<sub>7</sub>O<sub>18</sub>. An interpretation is inserted.

and comments on the manuscript. We are also grateful to Mrs Gunvor Winlöf for skilful technical assistance. The present study has been performed within a research program supported by the Swedish Natural Science Research Council. A grant from the Knut and Alice Wallenberg Foundation for the JEOL 200 CX electron microscope is gratefully acknowledged.

#### References

- ALLPRESS, J. G. & SANDERS, J. V. (1973). J. Appl. Cryst. 6, 165-190.
- ANDERSSON, S. (1965a). Acta Chem. Scand. 19, 557-563.
- ANDERSSON, S. (1965b). Acta Chem. Scand. 19, 2285-2290.
- ANDERSSON, S. (1965c). Bull. Soc. Chim. Fr. pp. 1088-1094.
- ANDERSSON, S. (1967a). Acta Chem. Scand. 21, 1777-1782.
- ANDERSSON, S. (1967b). Z. Anorg. Allg. Chem. 351, 106-112.
- APPENDINO, P. (1973). Annal. Chim. (Rome), 63, 547-556.
- BRUSSET, H., GILLIER-PANDRAUD, H. & BELLE, J.-P. (1967). Bull. Soc. Chim. Fr. pp. 2276–2283.

COWLEY, J. M. & MOODIE, A. F. (1957). Acta Cryst. 10, 609-619.

- GOODMAN, P. & MOODIE, A. F. (1974). Acta Cryst. A30, 280-290.
- HAMBLING, P. G. (1953). Acta Cryst. 6, 98.
- HÖRLIN, T., MARINDER, B.-O. & NYGREN, M. (1982). Rev. Chim. Minér. 19, 231–238.
- IIJIMA, S. (1973). Acta Cryst. A29, 18-24.
- JOHANSSON, K. E., PALM, T. & WERNER, P.-E. (1980). J. Phys. E, 13, 1289–1291.
- MARINDER, B.-O. (1983). In preparation.
- MARINDER, B.-O. & SUNDBERG, M. (1982). Proc. R. Microsc. Soc. 17, 38.
- SHAFER, M. W. & ROY, R. (1959). J. Am. Ceram. Soc. 42, 482-486.
- SHELDRICK, G. M. (1976). SHELX. A program for crystal structure determination. Univ. of Cambridge, England.
- SKARNULIS, A. J., LILJESTRAND, G. & KIHLBORG, L. (1979). Chem. Commun. Univ. Stockholm, No. 1.
- SMITH, G. S. & SNYDER, R. L. (1979). J. Appl. Cryst. 12, 60-65.
- SUNDBERG, M. & MARINDER, B.-O. (1983). In preparation.
- WERNER, P.-E. (1969). Ark. Kemi, 31, 513-516.
- YVON, K., JEITSCHKO, W. & PARTHÉ, E. (1977). J. Appl. Cryst. 10, 73-74.

Acta Cryst. (1984). B40, 86-92

## A Crystal Chemical Study of the System CsCl-NaCl-H<sub>2</sub>O; Structures of the CsCl Derivative Compounds Cs<sub>1-x</sub>(Na.H<sub>2</sub>O)<sub>x</sub>Cl, CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O, and Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O

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(Received 20 May 1983; accepted 19 October 1983)

#### Abstract

A restudy of the system CsCl-NaCl-H<sub>2</sub>O {previously described by Plyushchev, Tulinova, Kutznetsova, Korovin & Petrova [*Zh. Neorg. Khim.* (1957). **2**, 2212-2220; *J. Inorg. Chem. USSR* (1957). **2**, 357-368]} yielded a new compound, which was found by crystal

structure analysis to be CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O. The crystals  $(M_r = 321 \cdot 27)$  are monoclinic, space group I2/c, with cell dimensions (from Guinier–Hägg powder refinement)  $a = 13 \cdot 6235$  (16),  $b = 5 \cdot 8322$  (5),  $c = 10 \cdot 7053$  (12) Å,  $\beta = 91 \cdot 26$  (1)°,  $V = 850 \cdot 38$  (11) Å<sup>3</sup> (=12 × 70 \cdot 9 Å<sup>3</sup>), Z = 4,  $D_x = 2 \cdot 509$  g cm<sup>-3</sup>, Mo K $\alpha$ ,  $\lambda = 0 \cdot 7107$  Å,  $\mu = 50 \cdot 0$  cm<sup>-1</sup>, F(000) = 592.  $R = 0 \cdot 022$ 

0108-7681/84/020086-07\$01.50

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for 1135 independent reflections  $[I > 2\sigma(I)]$ . The structure consists of a slightly distorted cubic CsCl framework in which  $\frac{2}{3}$  of the Cs atoms are replaced by H<sub>2</sub>O molecules and Na atoms inserted in cubic Cl<sub>4</sub> face centers between pairs of H<sub>2</sub>O molecules, forming coiled  $(Na.H_2O)_n$  chains. This structural principle was found to account for the existence of the unusual solid-solution series  $Cs_{1-x}(Na.H_2O)_xCl$ , in which x can range from 0 to 0.43 at 298 K. These solid solutions contain H<sub>2</sub>O replacing Cs, with (Na,H<sub>2</sub>O), chains looped or coiled at random in the cubic structure. It was found that Ca behaves with H<sub>2</sub>O in a similar manner in the previously known compound Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O. Crystals ( $M_r = 483.73$ ) are triclinic, space group  $P\overline{1}$ , with cell dimensions (from Guinier-Hägg powder refinement) a =6.9038 (7), b = 7.5127(9), c = 5.8774(7) Å, $\alpha =$ 92.28 (1),  $\beta = 96.19$  (1),  $\gamma = 65.23$  (1)°, V = 275.17 (4) Å<sup>3</sup> (=4×68.8 Å<sup>3</sup>), Z = 1,  $D_x = 2.919$ ,  $D_m$ (Berman balance) = 2.89(2) g cm<sup>-3</sup>, Mo K $\alpha$ ,  $\mu$  =  $75.5 \text{ cm}^{-1}$ , F(000) = 218, R = 0.079 for 1477 independent reflections  $[I > 2\sigma(I)]$ . The structure is similar in principle to that of the Na compound, but discrete  $H_2O-Ca-H_2O$  groups are formed, isolated from each other. Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O is isostructural with Cs<sub>2</sub>MnCl<sub>4</sub>.2H<sub>2</sub>O and Rb<sub>2</sub>MnCl<sub>4</sub>.2H<sub>2</sub>O. (The JCPDS Diffraction File Nos. for CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O and Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O are: 34-1489 and 34-1490).

#### Introduction

The behavior of cesium in salt brines has become of considerable interest in connection with the proposed disposal of high-level radioactive wastes containing <sup>137</sup>Cs ( $t_{1/2} = 30$  y) in deep salt deposits. To broaden our knowledge of the influence of Cs on such brine systems, we have undertaken a detailed study of the system CsCl-NaCl-H<sub>2</sub>O. A previous study has been carried out and reported by Plyushchev, Tulinova, Kutznetsova, Korovin & Petrova (1957), but we have refined their work and revealed important new features. These include the discovery of the previously unsuspected compound CsCl.2NaCl.2H<sub>2</sub>O, and the determination that the (Cs, Na)Cl solid solution reported by Plyushchev *et al.* contains water according to the formulation Cs<sub>1-x</sub>(Na.H<sub>2</sub>O)<sub>x</sub>Cl.

As described by Chou, Romankiw, Evans & Konnert (1983), the solubility relationships in the ternary system CsCl-NaCl-H<sub>2</sub>O were measured at 298 K by visual polythermal and isothermal techniques in order to refine the results of Plyushchev, Tulinova, Kutznetsova, Korovin & Petrova (1957). The ternary diagram at 298 K based on the data of the latter authors is shown in Fig. 1. Two solid phases reported by Plyushchev *et al.* were: pure NaCl, containing no measurable dissolved CsCl; and CsCl, which apparently can incorporate more than 30 mol % NaCl in solid solution. The last observation is unexpected, because in the binary system NaCl-CsCl, measured and described by Zemczuzny & Rambach (1910), no detectable solid solution was found in either end member. Nevertheless, when we investigated this region of the system, we found that the tie lines did apparently extend to the NaCl-CsCl axis up to 43 mol %.

At the end of the solid-solution series, in a narrow solution composition range (within  $\pm 1$  %), there appeared large prismatic crystals of a wholly new phase. The colorless crystals decomposed in air within a few days, apparently through loss of water of crystallization. By crystal structure analysis, described below, the composition was determined to be CsCl.2NaCl.2H<sub>2</sub>O, or CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O. This result suggested that if the solid-solution phases near CsCl actually contained H<sub>2</sub>O in addition to NaCl, the peculiar properties of these phases would be accounted for. In fact, chemical analysis of carefully dried samples in the solid-solution range revealed that H<sub>2</sub>O is present in an amount equimolar to NaCl. Thus, it is found that CsCl and NaCl in the presence of  $H_2O$ extensively interact with each other.

Fig. 2 shows the CsCl-NaCl-H<sub>2</sub>O system at 298 K as revised by our studies: the physical chemical studies in the range 293–393 K by Chou & Lee (1983), and by Chou & Romankiw (1983); and the crystal chemical studies at 298 K described in this paper, and by Chou, Romankiw, Evans & Konnert (1983). The crystal chemical aspects of the study, namely, the crystal structure study of the new compound CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O and the solid-solution series Cs<sub>1-x</sub>(Na.H<sub>2</sub>O)<sub>x</sub>Cl, are described in this paper. The crystal structure of the related compound Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O is also presented. Preliminary reports have appeared as abstracts (Chou, Romankiw, Evans & Konnert, 1982; Evans, Konnert, Chou & Romankiw, 1982).



Fig. 1. The CsCl-NaCl-H<sub>2</sub>O system as determined by Plyushchev, Tulinova, Kutznetsova, Korovin & Petrova (1957). Graduations are in wt %.

### **Experimental procedures**

The techniques for preparing and treating solutions and crystals are described by Chou & Lee (1983), Chou & Romankiw (1983) and Chou *et al.* (1983). Crystals containing CsCl tend to be hygroscopic, and in high humidity may convert to a liquid. Generally, samples could be prepared for X-ray powder study in air, but for single-crystal study it was necessary to enclose the crystal together with a drop of mother liquor in thin-walled glass capillary tubes.

Powder patterns were prepared with the Guinier-Hägg technique, using Cu  $K\alpha_1$  radiation ( $\lambda = 1.54052$  Å) and an internal standard (CaF<sub>2</sub>, a = 5.4638 Å). These provided the data for the refinement by least-squares analysis of unit-cell parameters given in the *Abstract*.

For structure analysis, X-ray intensities were measured on an automated Picker four-circle singlecrystal diffractometer. For this study, no problems of diffuse or irregular reflection profiles were encountered, and reflections were scanned in a  $\theta$ -2 $\theta$  mode, bracketing the  $\alpha$  doublet by 1° on either side. Nbfiltered Mo  $K\alpha$  radiation was used, and a standard reflection monitored about once an hour. The conditions of data measurement and structure refinements of CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O and Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O are given in Tables 1 and 4, respectively. The isotropic extinction parameter was refined concurrently with the structure refinements. All calculations were carried out with the XRAY76 program system (Stewart, 1976). Scattering factors for Cs<sup>+</sup>, Na<sup>+</sup>, Ca<sup>2+</sup>, Cl<sup>-</sup> and O<sup>-</sup> were taken from the exponential forms given by Cromer & Mann (1968).

#### Cesium disodium trichloride dihydrate

Large, colorless, prismatic crystals, usually occurring as penetration twins with composition planes (100) and (001), form readily at 298 K from solutions containing CsCl and NaCl in the molar ratio of 1.38:1



Fig. 2. The revised CsCl-NaCl-H<sub>2</sub>O phase diagram as determined by Chou *et al.* (1983). Graduations are in wt %.

## Table 1. Experimental details for CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O

Crystal size: 0.14×0.10×0.4 mm

Corrections: Lorentz, polarization, absorption, dispersion, isotropic extinction

Reflections measured: ~2500; 1206 independent with  $2\theta < 60^{\circ}$  (Mo K $\alpha$  radiation)

Reflections used for refinement: 1135 with  $I > 2\sigma(I)$ ; weights  $w = 1/\sigma^2$  (from counting statistics)

Refinement: 42 variables; to R = 0.022,  $R_n = 0.024$  $(\Delta/\sigma)_{max}$ : 0.001

Table 2. Structure parameters and root-mean-square thermal motions of atoms in CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O

	$\bar{\boldsymbol{u}}^2 = \frac{1}{3} \sum_i \boldsymbol{U}_{ii}.$			
	x	у	Z	ū (Å)
Cs	0.25	0.25	0.25	0.177(1)
Na(1)	0	0	0	0.172(4)
Na(2)	0	0.6652(2)	0.25	0.171(4)
Cl(1)	0.15861 (3)	0.26673(10)	0.58579(5)	0.168(2)
CI(2)	0	0.18249(14)	0.25	0.164(2)
0	0.3941(1)	0.2049(3)	0.5741(2)	0.170(4)
H(1)	0.326 (3)	0.250(10)	0.580 (4)	0.17(3)
H(2)*	0.385(3)	0.073 (7)	0.519(4)	0.22(5)

\* Coordinates from difference map.

(the saturated solution contains 98.4 g CsCl and 24.8 g NaCl in 100 g H<sub>2</sub>O). The crystals are monoclinic, and were found by systematic extinctions on single-crystal precession photographs to belong to the space group I2/c or *Ic*. The unit-cell parameters given in the *Abstract* were refined by least-squares analysis of X-ray powder data obtained with the Guinier-Hägg focusing camera [for 58 reflections,  $\sigma(2\theta) = 0.014^{\circ}$ ]. The powder data have been deposited.\*

The crystal structure was solved in I2/c by the symbolic addition procedure. Initial interpretation of the result was hampered by the assumption of a false composition based on an incorrect density determination made on impure material (crystals were contaminated by overgrowths of the cubic solid solution phase). As soon as the nonhydrogen atoms were all correctly identified, the refinement (on F) converged rapidly and satisfactorily to R = 0.036. The assumed centrosymmetric space group was thus confirmed. When absorption corrections were recalculated using the proper absorption parameter ( $\mu = 50.0 \text{ cm}^{-1}$ ), the final refinement reached R = 0.023. The composition of the compound determined in this way was subsequently confirmed by chemical analysis of pure material (Chou et al., 1983). The structure parameters are listed in Table 2.

The determined structure, though apparently rather complex, is actually based on a simple and elegant

<sup>\*</sup> Powder data, anisotropic thermal parameters and structure factors for both compounds and stereoviews of both structures have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 38935 (29 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

Table 3. Interatomic distances (Å) in CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O

Cs-Cl(2)(×2)	3-4286 (4) Å	O-Cl(1)	3·1496 (19) Å
$-Cl(1)(\times 2)$	3.5339(6)	-Cl(1)	3.2322 (15)
$-Cl(1)(\times 2)$	3.6914(6)	-Cl(1)	3.6081 (15)
$-Cl(1)(\times 2)$	3.8313(7)	-CI(2)	3.6428 (19)
-O(×2)	3-8204(18)	-Cl(1)	3.7299 (22)
-O(×2)	3-9568 (20)	-CI(1)	3.7585 (19)
		-Cl(2)	3.8438 (19)
$Na(1) - Cl(1)(\times 2)$	2.8009 (5)	-Cl(2)	3.8464 (19)
Cl(2)(×2)	2.8802 (4)	-H(1)	0.97 (4)
-O(×2)	2.3932(17)	-H(2)	0.98 (4)
$Na(2) - Cl(1)(\times 2)$	2.8421 (5)		
-CI(2)	3.0092 (14)		
-Cl(2)	2.8230(14)		
-O(×2)	2-3584 (19)		

principle. The unit-cell volume is just 12 times larger than the cubic cell of CsCl ( $a = 4 \cdot 121$  Å). The Cl atoms in the monoclinic crystal all lie close to the nodes of the CsCl framework, but  $\frac{2}{3}$  of the Cs atoms are replaced by H<sub>2</sub>O molecules. Na atoms are then inserted in Cl<sub>4</sub> squares on cubic face centers between pairs of H<sub>2</sub>O molecules. Fig. 3 shows a projection of the structure along the *b* axis. The simple cubic Cl framework is shown as a line network, and the direction of view is along a cubic face diagonal ( $\sqrt{2a_{CSCl}}$  =  $5 \cdot 827$  Å;  $b_{mon} = 5 \cdot 831$  Å). The Cs atoms lie in layers normal to the cube diagonal (monoclinic *a* axis), and the Na atoms and H<sub>2</sub>O molecules form coiled chains extended parallel to the *c* axis.

The Cs atoms, in addition to the eight Cl atoms at the coordination-cube corners, have six next-nearest neighbors: two Cs atoms (as in cubic CsCl), and four  $H_2O$  molecules. The Cs- $H_2O$  interatomic distances are shown in Table 3.

Fig. 4 shows an oblique view of a portion of the structure showing how the  $-H_2O-Na-H_2O-Na$  chains lie side by side in a layer parallel to the *bc* plane. The interatomic distances in the structure are listed in Table 3. The distances Na-H<sub>2</sub>O (avg. 2.38 Å) and Na-Cl (avg. 2.84 Å; 2.82 Å in NaCl) are perfectly normal, and show a remarkably good fit of these substituents in a CsCl structure that is only slightly distorted. The H<sub>2</sub>O molecules are displaced from the



Fig. 3. Projection of the structure of  $CsNa_2Cl_3.2H_2O$  along the *b* axis. Cl atoms are not shown, but they are located at the nodes of the simple cubic lattice indicated by solid lines.

cube centers away from the Na atoms and toward an opposite cube edge. Here they participate with Cl in two Cl-H-O hydrogen bonds of length 3.145 and 3.242 Å, at an angle of  $84.2^{\circ}$ . All other H<sub>2</sub>O-Cl distances are greater than 3.6 Å. These hydrogen bonds must play an important role in stabilizing the structure.

Images of the two H atoms can be discerned at the expected locations in the electron density difference map, appearing as rather sharp peaks reaching a height of  $0.6 \text{ e} \text{ Å}^{-3}$ . A section containing the O and two Cl(1) positions is shown in Fig. 5, which shows the H maxima. An attempt to refine their positions by least-squares analysis showed an uncertainty of H position of more than 0.05 Å, and atom H(2) converges on a position which is 0.75 Å from O. The coordinates given in Table 2 are taken instead from the peak centers of Fig. 5, which conform well to the expected O-H bond lengths of the H<sub>2</sub>O molecule.

### Cesium-sodium-chloride cubic solid solution

Zemczuzny & Rambach (1910) found no detectable solid solution in either end member of the anhydrous system NaCl-CsCl. When we compared the unit-cell



Fig. 4. Oblique view of a portion of the structure of  $C_sNa_2Cl_3.2H_2O$  showing the arrangement of the  $(Na-H_2O)_n$  chains. The Cl framework is shown as in Fig. 3.



Fig. 5. Difference electron density section in the plane containing  $H_2O$  and 2Cl(1) atoms. Contours at 0.2, 0.3, 0.4, 0.5, 0.6 e Å<sup>-3</sup>. (A sharp minimum at the Cl atom is not shown.)

parameters for NaCl and CsCl cooled from a molten mixture containing 75 wt % NaCl only slight changes from established values [for NaCl, Swanson & Fuyat (1953); for CsCl, Pöyhönen & Ruuskanen (1964)] for the pure end members were found:

	NaCl	CsCl
Pure	5·6402 Å	4·1200 Å
Mixed melt	5.6423 (8)	4.1225 (4).

From these data we conclude that NaCl from mixed anhydrous melts does not contain more than 0.2 mol % CsCl in solid solution. The slight increase in the CsCl cell parameter is anomalous, but may be affected by water absorbed by deliquescence in the presence of NaCl.

In the aqueous system with which we are concerned, we found that the cubic cell parameter of CsCl is hardly affected by the introduction of NaCl into the crystal. For a series of cubic crystals that contained as much as 38 mol % NaCl, the cubic unitcell parameters showed a slight increase but persisted within the range  $4 \cdot 120 - 4 \cdot 123$  Å (see Fig. 5). As the molar volume of NaCl ( $44 \cdot 8$  Å<sup>3</sup>) is much smaller than that of CsCl ( $69 \cdot 9$  Å<sup>3</sup>), these solid solutions clearly must also contain H<sub>2</sub>O. This possibility was first suggested by the revelation of the crystal structure of CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O, which showed how units of NaCl.H<sub>2</sub>O can be introduced into the CsCl structure with only slight distortion.

Further information on the character of the solid solutions is provided by index-of-refraction measurements. The values fall regularly as NaCl content increases, but more rapidly than would be expected for anhydrous phases on the basis of molal refractivities (dashed line, Fig. 6). If we use refractivity o, & values derived from the separate components: k(NaCl) = 0.249, k(CsCl) = 0.161, and  $k(\text{H}_2\text{O}) =$ 0.348 (from average *n* of the compound), the Gladstone-Dale law,  $n-1 = D \sum k_i p_i$  (D = density, p = weight fraction), gives excellent agreement with observed refractive indices, provided H<sub>2</sub>O is included in the composition according to  $(1-x)(CsCl).x(NaCl).x(H_2O)$ , or  $Cs_{1-x}(Na.H_2O)_xCl$ (solid line, Fig. 6). Subsequent analyses of dried samples of the cubic solid solutions did in fact show the presence of H<sub>2</sub>O in equimolar amount of NaCl "<sup>25</sup> (Chou et al., 1983).

An attempt was made to find direct evidence for the introduction of Na at the site  $\frac{1}{23}$ ,0 in the cubic CsCl unit cell by measuring intensities from a crystal containing approximately 15 mol % NaCl. The crystal was ground into a sphere and all intensities measured with Mo K $\alpha$  radiation in one hemisphere in the range  $2\theta < 100^\circ$ . The independent data set contained 104 reflections. Refinement of thermal and extinction parameters with the assumption of full occupancy by CsCl led directly to R = 0.018. The difference map showed a weak maximum at  $\frac{1}{2}, \frac{1}{2}, 0$ , and an anomalously large depression at  $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$ , the Cs site. All attempts to introduce Na and H<sub>2</sub>O into a model for least-squares analysis of occupancy and thermal parameters failed because it was impossible to avoid many cross correlations greater than 0.85. Unfortunately, direct evidence for the presence of Na is marginal.

Nevertheless, we can now understand the structural basis for the solid solution  $Cs_{1-x}(Na.H_2O)_xCl$  in terms of the structural properties of the new compound. H<sub>2</sub>O, rather than Na (which is far too small), replaces Cs at the center of the Cl<sub>8</sub> cube, and at the same time Na atoms are inserted in the cube-face centers between pairs of H<sub>2</sub>O molecules. The Na atoms thus are octahedrally coordinated, forming  $NaCl_4(H_2O)_2$  groups. In this grouping, each Na must be associated with two H<sub>2</sub>O molecules, as Na at a cube-face center cannot be in contact with Cs at a body center. Thus, in order to maintain charge balance, randomly coiled chains of the type  $-Na-H_2O-$ Na-H<sub>2</sub>O- must be formed, which may be terminated by Cs vacancies, or be looped into rings. As the H<sub>2</sub>O molecule is strongly displaced toward one cube edge, both to form O-H-Cl hydrogen bonds and to allow room for Na-O contact, H<sub>2</sub>O can only associate with two Na atoms at right angles and not in a straight line. This restriction accounts for the coiled arrangement of the chains in the compound CsNa<sub>2</sub>Cl<sub>3</sub>.2H<sub>2</sub>O. A fragment of the solid-solution structure consisting of 18 cubic cells is depicted in Fig. 7.



Fig. 6. Unit-cell parameters and refractive indices of CsCl-NaCl.H<sub>2</sub>O solid-solution phases.

#### Dicesium calcium tetrachloride dihydrate

After the principles of the cesium-sodium-chloridewater structures became understood, it occurred to us that calcium might play a role similar to sodium in analogous structures. The system CsCl-CaCl<sub>2</sub>-H<sub>2</sub>O has also been studied by Plyushchev, Tulinova, Kutznetsova, Korovin & Shipetina (1957), and the ternary diagram representing their results is shown in Fig. 8. Three compounds were found, all previously known: CsCaCl<sub>3</sub>, Cs<sub>5</sub>CaCl<sub>7</sub>, and Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O. The hydrate, which is the one of interest to us, was first prepared and described by Jamieson (1917). No solidsolution phases appeared in the study by Plyushchev *et al.* 

We prepared  $Cs_2CaCl_4.2H_2O$  as large, prismatic, triclinic crystals from solutions containing stoichiometric concentrations of the components. They are triclinic, and their crystallographic data are given in the *Abstract*. The crystals commonly form contact twins on ( $\overline{101}$ ), which corresponds to a pseudocube face in the CsCl sublattice. This face also



Fig. 7. Oblique view of 18 CsCl unit cells showing probable random arrangement of  $(Na-H_2O)_n$  chains in the cubic solidsolution structure.



Fig. 8. The system CsCl-CaCl<sub>2</sub>-H<sub>2</sub>O as determined by Plyushchev, Tulinova, Kutznetsova, Korovin & Shipetina (1957). Graduations are in wt %.

### Table 4. Experimental details for Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O

Crystal size: 0.18 × 0.29 × 0.72 mm

- Corrections: Lorentz, polarization, absorption, dispersion, isotropic extinction
- Reflections measured: 1613 independent, with  $2\theta < 60^{\circ}$  (Mo Ka radiation) Reflections used for refinement: 1477 with  $I > 2\sigma(I)$ ; weights  $w = 1/\sigma^2$  (from counting statistics)

Refinement: 44 variables; to R = 0.079,  $R_w = 0.110$ 

 $(\Delta/\sigma)_{\rm max} = 0.25$ 

#### Table 5. Structure parameters and root-mean-square thermal motions of atoms in Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O

15.44

	$u^2 = \frac{1}{3} \sum_i U_{ii}.$			
	x	у	Z	ū (Å)
Cs	0.1568(1)	0.1207(1)	0.2557(1)	0.128(3)
Ca	0.5	0.5	0.5	0.08(2)
Cl(1)	0.6294 (4)	0.1697 (4)	0.2357 (5)	0.11 (1)
Cl(2)	0.1060 (4)	0.6324 (5)	0.2638 (5)	0.12(1)
0	0.3789(16)	0.3443 (15)	0.7582 (15)	0.16 (4)

shows perfect cleavage. X-ray powder data,\* were used to refine the unit-cell parameters [for 56 reflections,  $\sigma(2\theta) = 0.016^{\circ}$ ]. The intensity data showed pronounced acentric statistical distributions, so initially the space group was assumed to be P1. The Cs atom positions were obtained from a Patterson  $(E^2-1)$ map, and the structure built up with the aid of successive electron density maps. As atoms were added to the structure, it soon became apparent that the true symmetry is P1. The statistics were likely distorted by a large extinction effect, which suppressed strong reflections, especially at low Bragg angles. The structure refined smoothly in P1. The final structure parameters are listed in Table 5. A projection of the structure along the c axis is shown in Fig. 9.

Our expectation about the structure of this compound is fully confirmed: it consists of a cubic CsCl framework in which half the Cs atoms are replaced by  $H_2O$  molecules, and Ca atoms are inserted in cubic

\* See deposition footnote.



Fig. 9. Projection of the structure of Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O along the c axis. The Cl framework is depicted as in Fig. 3.

# Table 6 Interatomic distances (Å) in Co CoCL 240

-O(×2)

face centers between pairs of H<sub>2</sub>O molecules. Ca

atoms are coordinated octahedrally as  $CaCl_4(H_2O)_2$ .

Chain formation is not required for charge balance

in this structure, and the H<sub>2</sub>O-Ca-H<sub>2</sub>O groups are

isolated from each other. The cubic chlorine

framework is only a little more distorted than in the

Na compound. Hydrogen bonds are formed between

H<sub>2</sub>O molecules and the pair of Cl atoms at one cube

edge opposite the Ca atom, as in the Na compound.

containing CsCl that might follow a structural prin-

ciple similar to that found in this work led to two

other compounds: Cs<sub>2</sub>MnCl<sub>4</sub>.2H<sub>2</sub>O and Rb<sub>2</sub>Mn-

Cl<sub>4</sub>.2H<sub>2</sub>O. The structures of these crystals have been

reported by Jensen (1964). They are, in fact, isostruc-

tural with Cs<sub>2</sub>CaCl<sub>4</sub>.2H<sub>2</sub>O. After transforming

Jensen's unit cells by  $(00\overline{1}/100/0\overline{1}0)$ , they may be

compared with that given in the Abstract as follows:

A subsequent search for other double-salt hydrates

Table 6 lists the bond lengths in the structure.

2.367 (12)

Table 6.	e 6. Interatomic distances (Å) in Cs <sub>2</sub> CaCl <sub>4</sub> .2H <sub>2</sub> O			a (Å)	Cs <sub>2</sub> CaCl <sub>4</sub> .2H <sub>2</sub> O	Cs <sub>2</sub> MnCl <sub>4</sub> .2H <sub>2</sub> O	Rb <sub>2</sub> MnCl <sub>4</sub> .2H <sub>2</sub> O
$\begin{array}{c} Cs - Cl(1) \\ - Cl(2) \\ - Cl(2) \\ - Cl(2) \\ - Cl(1) \\ - Cl(1) \\ - Cl(2) \\ - Cl(2) \\ - Cl(2) \\ - Cl(1) \end{array}$	3-447 (3) Å 3-492 (3) 3-536 (3) 3-545 (3) 3-604 (3) 3-710 (4) 3-831 (4)	O-Cl(1) -Cl(2) -Cl(2) -Cl(1) -Cl(1) -Cl(2) -Cl(2) -Cl(2)	3-153 (9) Å 3-267 (12) 3-549 (9) 3-613 (10) 3-626 (13) 3-649 (13) 3-786 (9) 3-888 (13)	$b (\mathbf{A})  c (\mathbf{A})  c (\mathbf{A})  \alpha (^{\circ})  \beta (^{\circ})  \gamma (^{\circ})  V (\mathbf{A}^{3})$	7·513 5·877 92·28 96·13 65·23 275·2	7.27 5.74 92.2 95.7 67.0 254.6	6.48 7.01 5.66 92.3 95.2 66.7 232.3.
_0 _0 _0	3·824 (9) 3·833 (11) 4·151 (12)	$Ca-Cl(2)(\times 2)$ $-Cl(1)(\times 2)$	2·711 (3) 2·739 (3)	Сноц.	L-M. & LEE, R. D	<b>References</b> (1983) J. Chem. Fi	ng Data <b>28</b> 390-39

#### References

- CHOU, I.-M. & LEE, R. D. (1983). J. Chem. Eng. Data, 28, 390-393. CHOU, I.-M. & ROMANKIW, L. A. (1983). J. Chem. Eng. Data, 28, 396-398.
- CHOU, I.-M., ROMANKIW, L. A., EVANS, H. T. JR & KONNERT, J. A. (1982). Trans. Geophys. Union, 63, 465.
- CHOU, I.-M., ROMANKIW, L. A., EVANS, H. T. JR & KONNERT. J. A. (1983). J. Chem. Eng. Data, 28, 393-396.
- CROMER, D. T. & MANN, J. B. (1968). Acta Cryst. A24, 321-324. EVANS, H. T. JR, KONNERT, L. A., CHOU, I.-M. & ROMANKIW.
- L. A. (1982). Am. Crystallogr. Assoc. Progr. Abstr. 10, 32. JAMIESON, G. S. (1917), Am. J. Sci. 43, 67-68.
- JENSEN, S. J. (1964). Acta Chem. Scand. 18, 2085-2097.
- PLYUSHCHEV, V. E., TULINOVA, V. B., KUTZNETSOVA, G. P., KOROVIN, S. S. & PETROVA, R. G. (1957). Zh. Neorg. Khim. 2. 2212-2220; Engl. trans. J. Inorg. Chem. USSR, 2, 357-368.
- PLYUSHCHEV, V. E., TULINOVA, V. B., KUTZNETSOVA, G. P., KOROVIN, S. S. & SHIPETINA, N. S. (1957). Zh. Neorg. Khim. 2, 2654-2660; Engl. trans. J. Inorg. Chem. USSR, 2, 267-275.
- PÖYHÖNEN, J. & RUUSKANEN, A. (1964). Ann. Acad. Sci. Fenn. Ser. A, 6, No. 146, 1-12.
- STEWART, J. M. (1976). Editor, XRAY76. Tech. Rep. TR-446, Computer Science Center, Univ. of Maryland, College Park, Maryland.
- SWANSON, H. E. & FUYAT, R. K. (1953). Natl Bur. Stand. US Circ. 539, Vol. 11, 41-43.
- ZEMCZUZNY, S. & RAMBACH, F. (1910). Z. anorg. Chem. 65, 403-428.

Acta Cryst. (1984). B40, 92-96

4.165 (9)

# Electron Density Distribution in an Ilmenite-Type Crystal of Cobalt(II) Titanium(IV) Trioxide

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(Received 23 July 1983; accepted 25 October 1983)

#### Abstract

The electron density distribution in a crystal of CoTiO<sub>3</sub> has been investigated with the single-crystal X-ray diffraction method. Deformation densities were observed around the  $Co^{2+}$  ion, which is qualitatively explained with the high-spin electron configuration

of a  $d^7$  ion in an octahedral field. The Ti<sup>4+</sup> ion lies in a negative region of the deformation density map, and a positive peak exists on the threefold axis at a position 0.63 Å from the Ti<sup>4+</sup> ion towards the Co<sup>2+</sup> ion. It is proposed that these negative and positive peaks are caused by deformation of the electron cloud to shield the positive charge of the neighbouring  $Co^{2+}$ 

0108-7681/84/020092-05\$01.50 © 1984 International Union of Crystallography

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